

## Chapter 17 – Assessing Computer Performance

Which of the world's computers is the fastest? This apparently silly question has been the fodder for many news reports, especially in the computer engineering trade press. It may be the case that the title "world's fastest computer" brings some recognition to the company that produces the machine, or it may be that the title is just good press.

The above question should immediately point out the difficulty in asking it. What does it mean for a computer to be fast? How does one measure the speed of computers? In an age that prefers to express admirable qualities by numerical measures, how does one assign a numerical measure to the speed of a computer? What does one measure?

The final answer to all of these questions is somewhat disappointing. One begins with the application or set of applications that is to be run on the computer, and then derives a figure of merit that matches one's business objectives. In other words, the measure of "fast" depends on what an individual wants to do with the computer. However, we shall yield to the standard temptation and attempt a discussion of assessing computer performance.

As noted in the first chapter of this book, in the first part of the 1950's IBM undertook a project to make a computer that was at least one hundred times as fast as any computer in its product line at the time. What is not clear is how they intended to measure the speed and produce a number such that the value for one computer would be 100 times that of the other.

Here are some typical comments that reflect the modern interest in computer speed.

1. I want a better computer.
2. I want a faster computer.
3. I want a computer or network of computers that does more work.
4. I have the latest game in "World of Warcraft" and want a computer that can play it.

Again, we ask what does "better" or "faster" really mean. Can one devise a well accepted numerical quantification of either value. As noted above, it is sometimes the case that these questions are easily answered. For the gaming requirement, just play the game on a computer of that model and see if you get performance that is acceptable.

The reference to the gaming world brings home a point on performance. In games one needs both a fast computer and a great graphics card; the performance of the entire system matters.

### **The Need for Greater Performance**

Aside from the obvious need to run games with more complex plots and more detailed and realistic graphics, are there any other reasons to desire greater performance? We shall study supercomputers later. At one time supercomputers, such as the Cray 2 and the CDC Cyber 205, were the fastest computers on the planet. One distinguished computer scientist gave the following definition of a supercomputer. "It is a computer that is only one generation behind the computational needs of the day."

We should mention a historical fact in the development of computational power. During the "Cold War" between the Soviet Union and the United States, there were many races going on. There was the well-known missile race, the space race, and the race for the fastest computer. Occasionally supercomputers were built as a matter of national pride. More often, they were built because there was a problem that required that computational power.

What applications require such computational power?

1. Weather modeling. We would like to have weather predictions that are accurate up to two weeks after the prediction. This requires a great deal of computational power. It was not until the 1990's that the models had the Appalachian Mountains.
2. We would like to model the flight characteristics of an airplane design before we actually build it. We have a set of equations for the flow of air over the wings and fuselage of an aircraft and we know these produce accurate results.

The only problem here is that simulations using these exact equations would take hundreds of years for a typical airplane. Hence we run approximate solutions and hope for faster computers that allow us to run less-approximate solutions.

3. As hinted in the historical chapter of this textbook, the U.S. National Security Agency uses computers in an attempt to crack the ciphers of foreign governments. All ciphers can be broken by brute force if sufficient computational power can be applied to the task. The goal of cryptographers is to create ciphers that would require millions of years to crack, using any known algorithm. In this race between cryptographers and cryptanalysts, more computational power is always welcome.

### **The Job Mix**

The World of Warcraft example above is a good illustration of a job mix. Here the job mix is simple; just one job – run this game. This illustrates the very simple statement “The computer that runs your job fastest is the one that runs your job fastest”. In other words, measure its performance on your job.

Most computers run a mix of jobs; this is especially true for computers owned by a company or research lab, which service a number of users. In order to assess the suitability of a computer for such an environment, one needs a proper “job mix”, which is a set of computer programs that represent the computing need of one's organization. Your instructor once worked at Harvard College Observatory. The system administrator for our computer lab spent considerable effort in selecting a proper job mix, with which he intended to test computers that were candidates for replacing the existing one. This process involved detailed discussions with a large number of users, who (being physicists and astronomers) all assumed that they knew more about computers than he did. Remember that in the 1970's; this purchase was for a few hundred thousand dollars.

These days, few organizations have the time to specify a good job mix. The more common option is to use the results of commonly available **benchmarks**, which are job mixes tailored to common applications.

### **What Is Performance?**

Here we make the observation that the terms “high performance” and “fast” have various meanings, depending on the context in which the computer is used. In many applications, especially the old “batch mode” computing, the measure was the number of jobs per unit time. The more user jobs that could be processed, the better.

For a single computer running spreadsheets, the speed might be measured in the number of calculations per second. For computers that support process monitoring, the requirement is that the computer correctly assesses the process and takes corrective action (possibly to include warning a human operator) within the shortest possible time.

Some systems, called “**hard real time**”, are those in which there is a fixed time interval during which the computer must produce and answer or take corrective action. Examples of this are patient monitoring systems in hospitals and process controls in oil refineries. As an example, consider a process monitoring computer with a required response time of 15 seconds. There are two performance measures of interest.

1. Can it respond within the required 15 seconds? If not, it cannot be used.
2. How many processes can be monitored while guaranteeing the required 15 second response time for each process being monitored. The more, the better.

### **The Average (Mean) and Median**

In assessing performance, we often use one or more tools of arithmetic. We discuss these here. The problem starts with a list of  $N$  numbers ( $A_1, A_2, \dots, A_N$ ), with  $N \geq 2$ . For these problems, we shall assume that all are positive numbers:  $A_j > 0, 1 \leq j \leq N$ .

### **Arithmetic Mean and Median**

The most basic measures are the average (mean) and the median. The average is computed by the formula  $(A_1 + A_2 + \dots + A_N) / N$ . The median is the “value in the middle”. Half of the values are larger and half are smaller. For a small even number of values, there might be two candidate median values. For most distributions, the mean and the median are fairly close together. However, the two values can be wildly different. For example, there is a high-school class in the state of Washington in which the average income of its 100 members is about \$1,500,000 per year; that’s a lot of money. If the salary of Bill Gates and one of his cohorts at Microsoft are removed, the average becomes about \$50,000. This value is much closer to the median. Disclaimer: This example is from memory.

### **Weighted Averages,**

In certain averages, one might want to pay more attention to some values than others. For example, in assessing an instruction mix, one might want to give a weight to each instruction that corresponds to its percentage in the mix. Each of our numbers ( $A_1, A_2, \dots, A_N$ ), with  $N \geq 2$ , has an associated weight. So we have  $(A_1, A_2, \dots, A_N)$  and  $(W_1, W_2, \dots, W_N)$ . The weighted average is  $(W_1 \cdot A_1 + W_2 \cdot A_2 + \dots + W_N \cdot A_N) / (W_1 + W_2 + \dots + W_N)$ . If all the weights are equal, this value becomes the arithmetic mean.

Consider the table adapted from our discussion of RISC computers.

Language	Pascal	FORTRAN	Pascal	C	SAL	Average
Workload	Scientific	Student	System	System	System	
Assignment	74	67	45	38	42	53.2
Loop	4	3	5	3	4	3.8
Call	1	3	15	12	12	8.6
If	20	11	29	43	36	27.8
GOTO	2	9	--	3	--	4.7

The weighted average  $0.532 \cdot T_A + 0.038 \cdot T_L + 0.086 \cdot T_C + 0.278 \cdot T_I + 0.047 \cdot T_G$  to assess an ISA (Instruction Set Architecture) to support this job mix.

## The Geometric Mean and the Harmonic Mean

### Geometric Mean

The geometric mean is the Nth root of the product  $(A_1 \cdot A_2 \cdot \dots \cdot A_N)^{1/N}$ . It is generally applied only to positive numbers, as we are considering here. Some of the SPEC benchmarks (discussed later) report the geometric mean.

### Harmonic Mean

The harmonic mean is  $N / ((1/A_1) + (1/A_2) + \dots + (1/A_N))$ . This is more useful for averaging rates or speeds. As an example, suppose that you drive at 40 miles per hour for half the distance and 60 miles per hour for the other half. Your average speed is 48 miles per hour. If you drive 40 mph for half the **time** and 60 mph for half the **time**, the average is 50.

Example:

Drive 300 miles at 40 mph. The time taken is 7.5 hours.

Drive 300 miles at 60 mph. The time taken is 5.0 hours.

You have covered 600 miles in 12.5 hours, for an average speed of 48 mph.

But: Drive 1 hour at 40 mph. You cover 40 miles

Drive 1 hour at 60 mph. You cover 60 miles. That is 100 miles in 2 hours; 50 mph.

### Measuring Execution Time

Whatever it is, performance is inversely related to execution time. The longer the execution time, the less the performance. Again, we assess a computer's performance by measuring the time to execute a single program or a mix of computer programs, the "job mix", which represents the computing work done at a particular location.

If a faster computer is better, how do we measure the speed? There are two measures in common use wall clock time and CPU execution time. In **wall-clock time** one starts the program and note the time on the clock. When the program ends, again note the time on the clock. The difference is the execution time. This is the easiest to measure, but the time measured may include time that the processor spends on other users' programs (it is time-shared), on operating system functions, and similar tasks. Nevertheless, it can be useful.

Some people prefer to measure the **CPU Execution Time**, which is the time the CPU spends on the single program. This is often difficult to estimate based on clock time.

### Reporting Performance: MIPS, MFLOPS, etc.

While we shall focus on the use of benchmark results to report computer performance, we should note that there are a number of other measures that have been used. The first is MIPS (**M**illion **I**nstructions **p**er **S**econd). Another measure is the FLOPS sequence, commonly used to specify the performance of supercomputers, which tend to use floating-point math fairly heavily. The sequence is:

MFLOPS	Million Floating Point Operations per Second
GFLOPS	Billion Floating Point Operations Per Second (The term "giga" is the standard prefix for $10^9$ .)
TFLOPS	Trillion Floating Point Operations Per Second (The term "tera" is the standard prefix for $10^{12}$ .)

### Using MIPS as a Performance Measure

There are a number of reasons why this measure has fallen out of favor. One of the main reasons is that the term “MIPS” had its origin in the marketing departments of IBM and DEC, to sell the IBM 370/158 and VAX-11/780. One wag has suggested that the term “MIPS” stands for “**M**eaningless **I**ndicator of **P**erformance for **S**alesmen”.

A more significant reason for the decline in the popularity of the term “MIPS” is the fact that it just measures the number of instructions executed and not what these do. Part of the RISC movement was to simplify the instruction set so that instructions could be executed at a higher clock rate. As a result the RISC designs might have a higher MIPS rating, but do less work, as each instruction does less work.

For example, consider the instruction  $A[K++] = B$  as part of a loop. The VAX supports an auto-increment mode, which uses a single instruction to store the value into the array and increment the index. Most RISC designs require two instructions to do this. Put another way, in order to do an equivalent amount of work a RISC machine must run at a higher MIPS rating than a CISC machine. However, the measure does have merit when comparing two computers with identical organization.

### GFLOPS, TFLOPS, and PFLOPS

The term “PFLOP” stands for “Petaflop” or  $10^{15}$  floating-point operations per second. This is the next goal for the supercomputer community. The supercomputer community prefers this measure, due mostly to the great importance of floating-point calculations in their applications. A typical large-scale simulation may devote 70% to 90% of its resources to floating-point calculations.

The supercomputer community has spent quite some time in an attempt to give a precise definition to the term “floating point operation”. As an example, consider the following code fragment, which is written in a standard variety of the FORTRAN language.

```
DO 200 J = 1, 10
200 C(J) = A(J)*B(J) + X
```

The standard argument is that the loop represents only two floating-point operations: the multiplication and the addition. I can see the logic, but have no other comment. The main result of this measurement scheme is that it will be difficult to compare the performance of the historic supercomputers, such as the CDC Cyber 205 and the Cray 2, to the performance of the modern day “champs” such as a 4 GHz Pentium 4.

In another lecture we shall investigate another use of the term “flop” in describing the classical supercomputers, when we ask “What happened to the Cray 3?”

### CPU Performance and Its Factors

The CPU **clock cycle time** is possibly the most important factor in determining the performance of the CPU. If the clock rate can be increased, the CPU is faster. In modern computers, the clock cycle time is specified indirectly by specifying the clock cycle rate. Common clock rates (speeds) today include 2GHz, 2.5GHz, and 3.2 GHz. The clock cycle times, when given, need to be quoted in picoseconds, where 1 picosecond =  $10^{-12}$  second; 1 nanosecond = 1000 picoseconds.

The following table gives approximate conversions between clock rates and clock times.

Rate	Clock Time	
1 GHz	1 nanosecond	= 1000 picoseconds
2 GHz	0.5 nanosecond	= 500 picoseconds
2.5 GHz	0.4 nanosecond	= 400 picoseconds
3.2 GHz	0.3125 nanosecond	= 312.5 picoseconds
4.0 GHz	0.250 nanosecond	= 250 picoseconds

We shall return later to factors that determine the clock rate in a modern CPU. There is much more to the decision than “crank up the clock rate until the CPU fails and then back it off a bit”. As mentioned in an earlier chapter, the problem of cooling the chip has given rise to limits on the clock speed, called the “**power wall**”. We shall say much more on this later.

### **CPI: Clock Cycles per Instruction**

This is the number of clock cycles, on average, that the CPU requires to execute an instruction. We shall later see a revision to this definition. Consider the Boz-7 design used in my offerings of CPSC 5155. Each instruction would take 1, 2, or 3 major cycles to execute: 4, 8, or 12 clock cycles. In the Boz-7, the instructions referencing memory could take either 8 or 12 clock cycles, those that did not reference memory took 4 clock cycles. A typical Boz-7 instruction mix might have 33% memory references, of which 25% would involve indirect references (requiring all 12 clock cycles).

$$\begin{aligned} \text{The CPI for this mix is } \text{CPI} &= (2/3) \bullet 4 + 1/3 \bullet (3/4 \bullet 8 + 1/4 \bullet 12) \\ &= (2/3) \bullet 4 + 1/3 \bullet (6 + 3) \\ &= 8/3 + 3 = 17/3 = 5.33. \end{aligned}$$

The Boz-7 has such a high CPI because it is a traditional fetch-execute design. Each instruction is first fetched and then executed. Adding a prefetch unit on the Boz-7 would allow the next instruction to be fetched while the present one is being executed. This removes the three clock cycle penalty for instruction fetch, so that the number of clock cycles per instruction may now be 1, 5, or 9.

$$\begin{aligned} \text{For this CPI} &= (2/3) \bullet 1 + 1/3 \bullet (3/4 \bullet 5 + 1/4 \bullet 9) = 2/3 + 1/3 \bullet (15/4 \bullet + 9/4) \\ &= 2/3 + 1/3 \bullet (24/4) = 2/3 + 1/3 \bullet 6 = 2.67. \text{ This is still slow.} \end{aligned}$$

### **More on Benchmarks**

As noted above, the best benchmark for a particular user is that user’s job mix. Only a few users have the resources to run their own benchmarks on a number of candidate computers. This task is now left to larger test labs. These test labs have evolved a number of **synthetic benchmarks** to handle the tests. These benchmarks are job mixes intended to be representative of real job mixes. They are called “synthetic” because they usually do not represent an actual workload.

The **Whetstone** benchmark was first published in 1976 by Harold J. Curnow and Brian A. Wichman of the British National Physical Laboratory. It is a set of floating-point intensive applications with many calls to library routines for computing trigonometric and exponential functions. Supposedly, it represents a scientific work load. Results of this are reported as

KWIPS (Thousand Whetstone Instructions per Second), or  
 MWIPS (Million Whetstone Instructions per Second)

The Linpack (**Linear Algebra Package**) benchmark is a collection of subroutines to solve linear equations using double-precision floating-point arithmetic. It was published in 1984 by a group from Argonne National Laboratory. Originally in FORTRAN 77, it has been rewritten in both C and Java, with results reported in FLOPS, GFLOPS, TFLOPS, etc.

### **Games People Play (with Benchmarks)**

Synthetic benchmarks (Whetstone, Linpack, and Dhrystone) are convenient, but easy to fool. These problems arise directly from the commercial pressures to quote good benchmark numbers in advertising copy. This problem is seen in two areas.

1. Manufacturers can equip their compilers with special switches to emit code that is tailored to optimize a given benchmark at the cost of slower performance on a more general job mix. “Just get us some good numbers!”
2. The benchmarks are usually small enough to be run out of cache memory. This says nothing of the efficiency of the entire memory system, which must include cache memory, main memory, and support for virtual memory.

There are rumors about a 1995 Intel special compiler that was designed only to excel in the SPEC integer benchmark. Its code was fast, but incorrect.

**Bottom Line:** Small benchmarks invite companies to fudge their results. Of course they would say “present our products in the best light.”

### **More Games People Play (with Benchmarks)**

Your instructor recalls a similar event in the world of Lisp machines. These were specialized workstations designed to optimize the execution of the LISP language widely used in artificial intelligence applications. The two “big dogs” in this arena were Symbolics and LMI (Lisp Machines Incorporated). Each of these companies produced a high-performance Lisp machine based on a microcoded control unit. These were the Symbolics-3670 and the LMI-1. Each company submitted its product for testing by a graduate student who was writing his Ph.D. dissertation on benchmarking Lisp machines.

Between the time of the first test and the first report at formal conference, LMI customized its microcode for efficient operation on the benchmark code. At the original test, the LMI-1 had only 50% of the performance of the Symbolics-3670. By the time of the conference, the LMI-1 was now “officially” 10% faster. The managers from Symbolics, Inc. complained loudly that the new results were meaningless. However, these complaints were not necessary as every attendee at the conference knew what had happened and acknowledged the Symbolics-3670 as faster. Note: Neither design survived the Intel 80386, which was much cheaper than the specialized machines, had an equivalent GUI, and was about as fast. At the time, the costs were about \$6,000 vs. about \$100,000.

### **The SPEC Benchmarks**

The SPEC (Standard Performance Evaluation Corporation) was founded in 1988 by a consortium of computer manufacturers in cooperation with the publisher of the trade magazine *The Electrical Engineering Times*. (See [www.spec.org](http://www.spec.org))

As of 2007, the current SPEC benchmarks were:

1. CPU2006            measures CPU throughput, cache and memory access speed, and compiler efficiency. This has two components:  
                           SPECint2006 to test integer processing, and  
                           SPECfp2006 to test floating point processing.
2. SPEC MPI 2007    measures the performance of parallel computing systems and clusters running MPI (Message–Passing Interface) applications.
3. SPECweb2005     a set of benchmarks for web servers, using both HTTP and HTTPS.
4. SPEC JBB2005     a set of benchmarks for server–side Java performance.
5. SPEC JVM98       a set of benchmarks for client–side Java performance.
6. SPEC MAIL 2001 a set of benchmarks for mail servers.

The student should check the SPEC website for a listing of more benchmarks.

### **Some Concluding Remarks on Benchmarks**

First, remember the great temptation to manipulate benchmark results for commercial advantage. As the Romans said, “Caveat emptor.” Also remember to read the benchmark results skeptically and choose the benchmark that most closely resembles your own workload. As the English say, “Let the buyer beware.”

Finally, do not forget **Amdahl’s Law**, which computes the improvement in overall system performance due to the improvement in a specific component. This law was formulated by George Amdahl in 1967. One formulation of the law is given in the following equation.

$$S = 1 / [ (1 - f) + (f/k) ]$$

where            S is the speedup of the overall system,  
                       f is the fraction of work performed by the faster component, and  
                       k is the speedup of the new component.

It is important to note that as the new component becomes arbitrarily fast ( $k \rightarrow \infty$ ), the speedup approaches the limit  $S_{\infty} = 1/(1 - f)$ .

If the newer and faster component does only 50% of the work, the maximum speedup is 2. The system will never exceed being twice as fast due to this modification.